

Physics Notes

BY

Er. Lalit Sharma

B.Tech (Electrical)

Ex. Lecturer Govt. Engg. College Bathinda

Physics Faculty Ranker's Point, Bathinda

Arun Garg

M.Sc. Physics

Gold Medalist

Physics Faculty Ranker's Point, Bathinda

Class:10+2

Unit: III

Topic: Magnetic Effects of Current and Magnetism

SYLLABUS: UNIT-III-B

Concept of magnetic field, Oersted's experiment, Biot-Savart law, magnetic field due to an infinitely long current carrying straight wire and a circular loop; Ampere's circuit law and its applications to straight and toroidal solenoids; Force on a moving charge in uniform magnetic and electric fields, Cyclotron; Force on current – carrying conductor in a uniform magnetic field. Forces between two parallel current- carrying conductors- definition of ampere; Torque experienced by a current loop in a uniform magnetic field, moving coil galvanometer- its current sensitivity and conversion to ammeter and voltmeter.

Current loop as a magnetic dipole and its magnetic dipole moment; Magnetic dipole moment of a revolving electron; Magnetic field intensity due to magnetic dipole (bar magnet) along the axis and perpendicular to the axis; Torque on a magnetic dipole (bar magnet) in a uniform magnetic field; Bar magnet as an equivalent solenoid, Magnetic field lines' Earth's magnetic field and magnetic elements; Para-dia and ferro-magnetic substances with examples, Electromagnets and permanent magnets.

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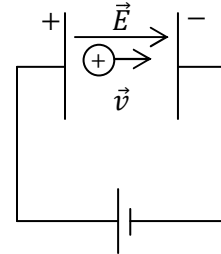
Q.1. Discuss motion of charged particle in Electric Field for

- i) $\theta = 0^\circ$
- ii) $\theta = 180^\circ$
- iii) $\theta = 90^\circ$

θ is the angle between \vec{V} and \vec{E} .

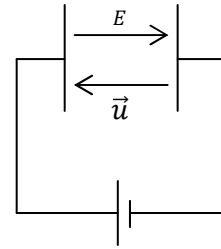
Ans. Case I:- $\theta = 0^\circ$

$$\begin{aligned} \vec{V} &= \vec{u} + \vec{a}t \quad \left[\text{acc, } a = \frac{(q\vec{E})}{m} \right] \\ &= \vec{u} + \frac{(q\vec{E})}{m} \cdot t \\ &= \vec{u} + \frac{(q\vec{E})}{m} \cdot t \\ &= \vec{u} + \frac{qt}{m} \cdot \vec{E} \quad [\text{speed increases, K.E. increases}] \end{aligned}$$



Case II:- $\theta = 180^\circ$

$$\begin{aligned} \vec{V} &= \vec{u} + \vec{a}t \\ &= \vec{u} + \frac{(q\vec{E})}{m} \cdot t \end{aligned}$$



Speed decreases till the particles speed becomes zero and then increases.

Initial horizontal speed = u

$$x = u_x \cdot t + \frac{1}{2} a_x t^2$$

$$x = u_x \cdot t \quad \text{----- } (i)$$

$$y = u_y \cdot t + \frac{1}{2} \cdot a_y \cdot t^2$$

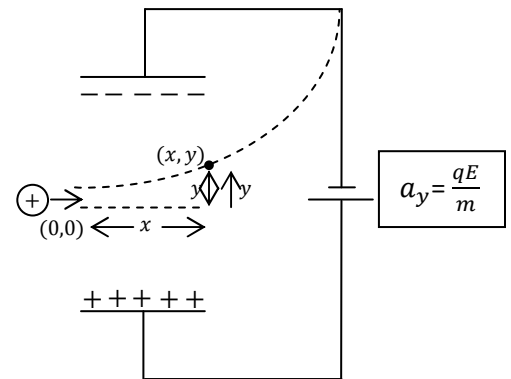
$$y = 0 + \frac{1}{2} \cdot a_y \cdot t^2$$

$$y = 0 + \frac{1}{2} \cdot a_y \cdot \left(\frac{x}{u}\right)^2$$

$$\boxed{t = \frac{x}{u}} \text{ from } (i)$$

$$y = \frac{1}{2} \cdot \left(\frac{q\vec{E}}{m}\right) \cdot \frac{x^2}{u^2}$$

$$y = (\text{constant}) \cdot x^2$$



3

Q2. Discuss motion of charged particle in magnetic field for

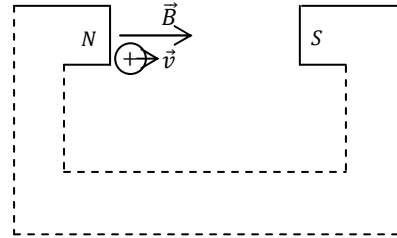
- i) $\theta = 0^\circ$
- ii) $\theta = 180^\circ$
- iii) $\theta = 90^\circ$

θ is the angle between \vec{V} and \vec{B} .

Ans. $\vec{F} = q(\vec{V} \times \vec{B})$

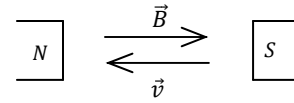
Case I:- $\theta = 0^\circ$
 $F = qVB \sin \theta$
 $= qVB \sin 0$

$F = 0$



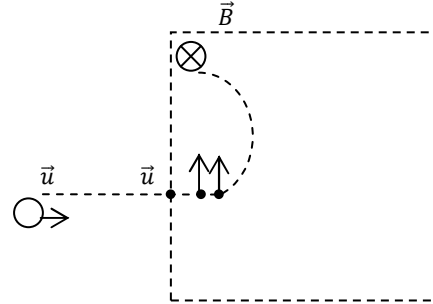
Case II:- $\theta = 180^\circ$
 $\vec{F} = q(\vec{V} \times \vec{B})$
 $\vec{F} = qVB \sin 180^\circ$

$F = 0$



Case III:- $\vec{V} \perp \vec{B}$
 $\vec{F} = q(\vec{V} \times \vec{B})$
 $\vec{F} = qVB \sin 90^\circ$

$F = qVB$

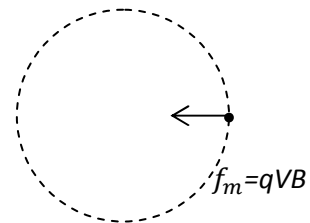


Towards centre of circle
 \perp to \vec{V} , \perp to \vec{B}

$$qVB = \frac{mv^2}{r}$$

$$\frac{qBr}{m} = v$$

$$T = \frac{2\pi r}{v} = \frac{2\pi r}{\frac{qBr}{m}} = \frac{2\pi m}{qB} \quad \boxed{T = \frac{2\pi m}{qB}}$$



5

Q3. Working of 'Velocity Selector' switch?

Ans. Electric Field causes downward deflection of a charged particle.
Magnetic Field causes upward deflection of a charged particle.

For no deflection of particle, upward force must be equal to downward force.

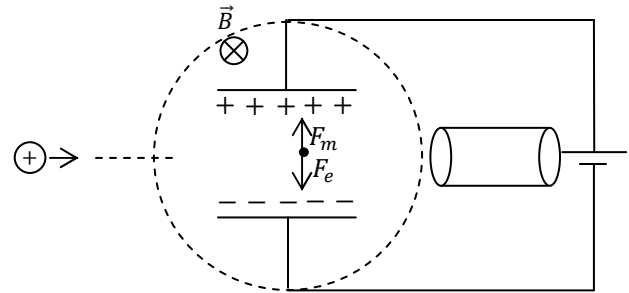
$$F_E = qE \quad \text{-----} \quad \textcircled{1}$$

$$F_m = qVB \quad \text{-----} \quad \textcircled{2}$$

$$qE = qVB$$

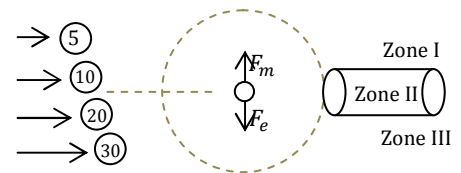
$$E = VB$$

$v = \frac{E}{B}$



Example:- $= \frac{100}{5} = 20\text{m/sec}$

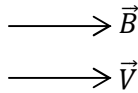
Particles moving with speed 20m/sec will enter the box. (Zone II)
 Particles with speed less than 20 *i.e.* with 5 and 10 will get deflected towards Zone III.
 Particles with speed 30 will enter Zone I.



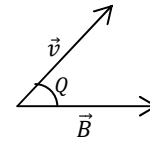
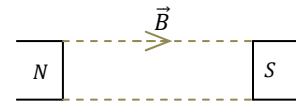
Q4. Find time period and pitch of helical path followed by a charged particle when it enters at angle θ with B .

Ans.1. Horizontal component

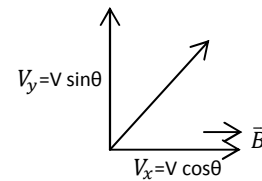
$$V_{\parallel} = V \cos\theta \text{ is parallel to } \vec{B}$$



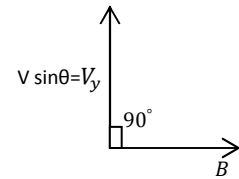
So, force acting due to $V \cos\theta$ is zero.



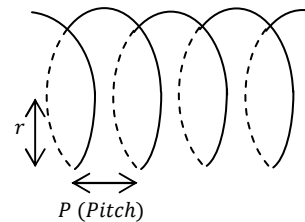
No acceleration along x-axis particle moves with constant speed $V \cos\theta$.



2. $V_y = V \sin\theta$ causes circular motion.



3. $T = \frac{2\pi r}{V_y} = \frac{2\pi r}{V \sin\theta}$



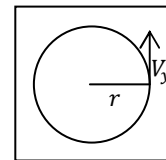
4. Pitch: The distance between two identical points is called pitch.

$$P = V_x \times T$$

$$= V_x \left(\frac{2\pi r}{V \sin\theta} \right)$$

$$P = 2\pi r \frac{V \cos\theta}{V \sin\theta} = 2\pi r \cot\theta$$

$$P = 2\pi r \cot\theta$$



Q5. Discuss construction and working of Cyclotron?

Ans.a) **Principle:-**

Cyclotron is a device used to increase speed/Kinetic Energy where

E is used to increase speed.

B is used to change direction.

($E \rightarrow$ Electric Field, $B \rightarrow$ Magnetic Field).

b) **Construction:-**

Two magnets are used to create magnetic fields. E (alternating) is applied across the two D's as shown in figure.

Plane of D's is \perp to B .

c) **Working:-**

Particle is at R (say particle is $-ve$ charged). Disc D_2 is made $+ve$. Particle moves to position S with increase speed. Particle moves from S to J with constant speed, but its direction changes due to magnetic field. Now D_1 becomes $+ve$ when particle is at J , particle jumps to K with increase in speed due to *Electric Jerk*.

speed of particle increase with increase in radius, When radius of particle circle is almost equal to the disc radius, particle is taken out of the window w .

d) **Radius, Kinetic Energy:-**

$$qvB = \frac{mv^2}{r}$$

$$r = \frac{mv}{qB}$$

$$\boxed{r = \frac{mv}{qB}}, \quad v = \frac{rqB}{m}$$

As speed increase, radius also increase. \rightarrow

$$K.E_{max} = \frac{1}{2}mv_{max}^2$$

$$= \frac{1}{2}m \left(\frac{qB r_{max}}{m} \right)^2$$

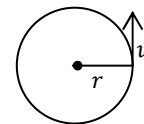
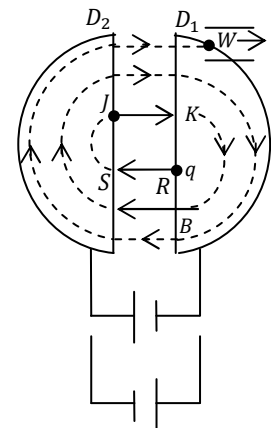
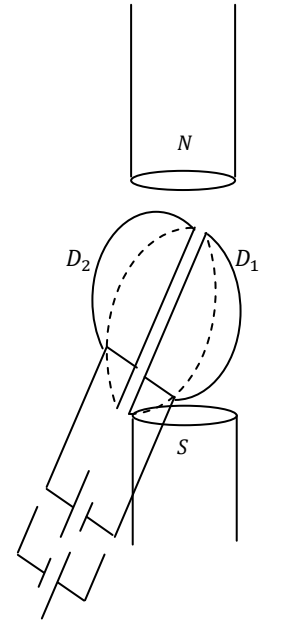
$$= \frac{1}{2}m \left(\frac{q^2 B^2 r_{max}^2}{m^2} \right)$$

$$\boxed{K.E_{max} = \frac{1}{2} \left(\frac{q^2 B^2 r_{max}^2}{m} \right)}$$

$$K.E_{max} \propto r_{max}^2$$

$$T_{1/2} = \frac{\pi r}{v} = \frac{\pi \times m}{qB} \quad \boxed{T_{1/2} = \frac{\pi m}{qB}}$$

$T_{1/2} \rightarrow$ Time of stay of particle in one D



Q6. Derive an expression for force on a current carrying conductor placed in a magnetic field.

OR

Prove $\vec{F} = I(\vec{l} \times \vec{B})$.

Ans. A charged particle q experiences a force $\vec{F} = q(\vec{V} \times \vec{B})$ when placed in a magnetic field.

A current is equivalent to number of charges in motion.

Force on each charge $\Rightarrow F$

$$F = qVB$$

No. of charges in conductor,

$$N = (n) A l$$

$$F_{net} = NF$$

$$= (n A l) (qVB)$$

$$= (nAqV) l B$$

$$F_{net} = I \cdot l \cdot B$$

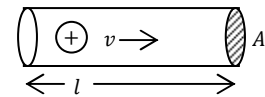
$$\vec{F}_{net} = I (\vec{l} \times \vec{B})$$

Direction:- Fleming's **left hand** rule

First Finger \rightarrow Field
 Second Finger \rightarrow Current
 Thumb Finger \rightarrow motion or Force

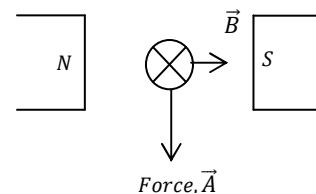
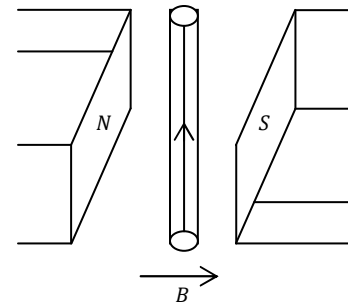
Example:- Downward Force (Left hand rule)

Current flows inwards, Magnetic Field towards right, Force downwards.



$n \rightarrow$ no. of e/volume

$$I = nAqVd$$



Q7. Find $\frac{\text{Force}}{\text{length}}$ between two infinite conductor carrying I_1 and I_2 and separated by distance d .

$$\frac{F}{l} = \frac{\mu_0 I_1 I_2}{2\pi d}$$

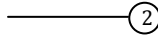
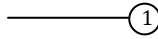
Ans.

Step 1. Current carried by conductor of length dl is I_2

$$dF = I (\vec{dl} \times \vec{B})$$

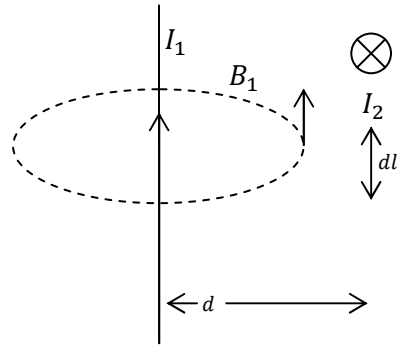
$$dF_2 = I_2 (\vec{dl} \times \vec{B})$$

$$dF_2 = I_2 dl B_1$$



Step 2.

$$B_1 = \frac{\mu_0 I_1}{2\pi d}$$



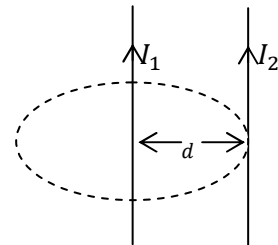
Step 3.

$$dF = I_2 \cdot dl B_1$$

$$= I_2 dl \left(\frac{\mu_0 I_1}{2\pi d} \right)$$

$$\frac{dF}{dl} = \frac{I_2 \cdot \mu_0 \cdot I_1}{2 \cdot \pi \cdot d}$$

$$\frac{\text{Force}}{\text{length}} = \frac{\mu_0 \cdot I_1 \cdot I_2}{2 \cdot \pi \cdot d}$$

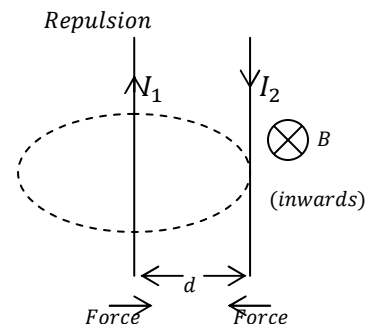
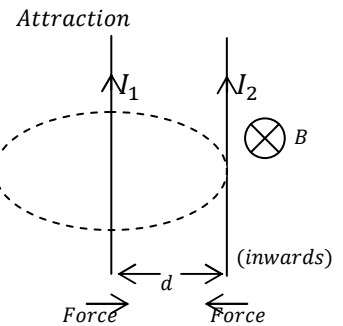


They both attract each other. According to left hand Flemings rule, current is upwards, Magnetic Field inwards, force towards the conductor carrying current I_1 (i.e. towards left).

Two possible cases:-

Case I:- If two currents I_1 and I_2 are in same direction, two conductors will attract each other.

Case II:- If two currents I_1 and I_2 are in opposite direction, two conductors will repel each other.



Q8. Derive an expression for Torque on a current carrying loop placed in a magnetic field?

OR

**Prove $\vec{\tau} = \vec{M} \times \vec{B}$ where $M = I \vec{A}$
 $= I \vec{A} \times \vec{B}$**

Ans.

Step 1.

Force on PQ and RS

$$F = BIl$$

$$\vec{F}_{PQ} = BIl \text{ (upwards)}$$

$$\vec{F}_{RS} = BIl \text{ (downwards)}$$

$$|\vec{\tau}| = 2 |\vec{r} \times \vec{F}|$$

$$= 2r F \sin\theta$$

$$= 2r BIl \sin\theta$$

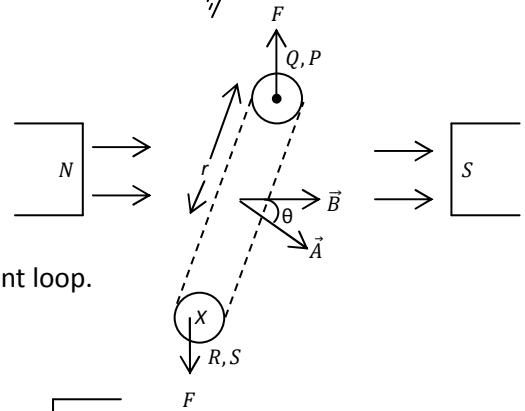
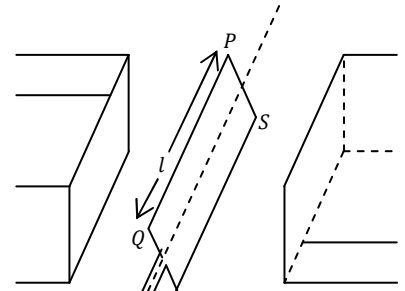
$$= b IBl \sin\theta$$

$$\vec{\tau} = IAB \sin\theta$$

$$= MB \sin\theta$$

$$\vec{\tau} = \vec{M} \times \vec{B}$$

[2r = breadth]



Where $M = NIA$ is the magnet moment of current loop.

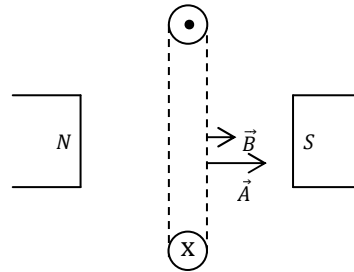
Discussion:-

Case I:-

$$\theta = 0^\circ$$

$$\tau = MB \sin\theta$$

$$\tau_{min} = 0$$



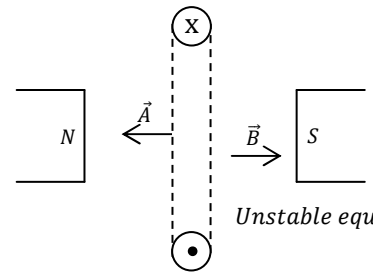
Stable equilibrium

Case II:-

$$\theta = 180^\circ$$

$$\tau = MB \sin\theta$$

$$\tau_{min} = 0$$



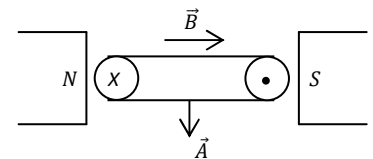
Unstable equilibrium

Case III:-

$$\theta = 90^\circ$$

$$\tau = MB \sin\theta$$

$$\tau_{max} = MB$$



Q9. Explain Principle, Construction and Working of moving coil galvanometer?

Ans.a) **Principle:-**

Galvanometer work on the principle that deflection produced in current carrying coil is proportional to current in coil.

i.e. $\theta \propto I$

b) **Construction:-**

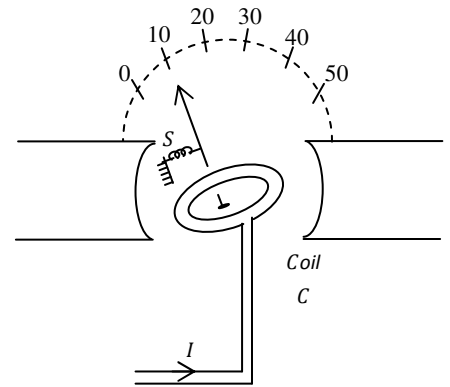
Magnets of the given shape are used to produce radial magnetic field. For radial magnetic field $\vec{A} \perp \vec{B}$ for all positions of the coil plane.

$$\tau = MB \sin 90^\circ$$

$$\tau = MB$$

Coil C carries current I . Any deflection produced in coil is measured by "needle" on the scale.

Spring S provides necessary torque in opposite direction to make the needle stable.



c) **Working:-**

Current in the coil develops clockwise torque (say)

$$\tau_c = MB \sin 90^\circ$$

$$\tau_c = (NIA) B \times I \quad \text{--- (1)}$$

Spring provides anticlockwise torque (say)

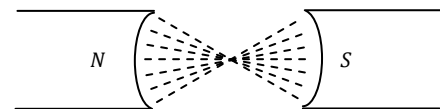
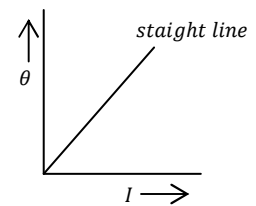
$$\tau_{ac} = K\theta \quad \text{--- (2)}$$

Needle is stable when

$$\tau_{ac} = \tau_c \quad \text{[Anticlockwise torque = clockwise torque]}$$

$$K\theta = nIAB$$

$$\theta = \left(\frac{nAB}{K}\right) \cdot I$$



Sensitivity

a) sensitivity : $\frac{\Delta \text{output}}{\Delta \text{input}}$

b) Current sensitivity: $\frac{\Delta \theta}{\Delta I}$

$$\text{Current sensitivity} = \frac{nAB}{K}$$

c) Voltage sensitivity = $\frac{\Delta \theta}{\Delta V} = \frac{\Delta \theta}{R \Delta I}$
 $= \frac{1}{R} \left(\frac{nAB}{K}\right)$

$$\text{Voltage sensitivity} = \frac{\text{current sensitivity}}{R}$$

Q10. Convert a galvanometer of 1mA, 1KΩ to
a) Ammeter of (0-1) Amp.
b) Voltmeter of (0-100) volt

Ans. Galvanometer

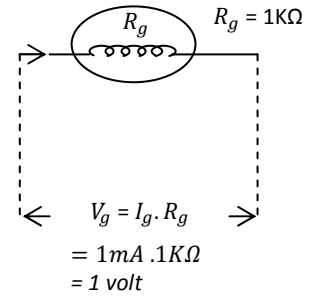
So, given galvanometer can act as ammeter of

1 m A

OR

Can act as voltmeter of

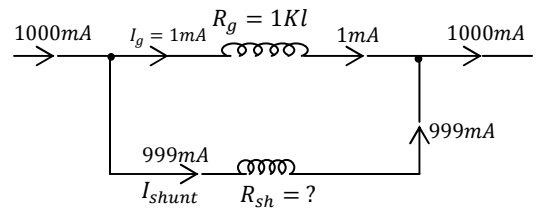
1 volt



a) In parallel, voltage is same.

$$I_g \cdot R_g = I_{sh} \cdot R_{sh}$$

$$R_{sh} = \frac{1mA \cdot 1K\Omega}{999} = \frac{1000}{999} = 1\Omega$$



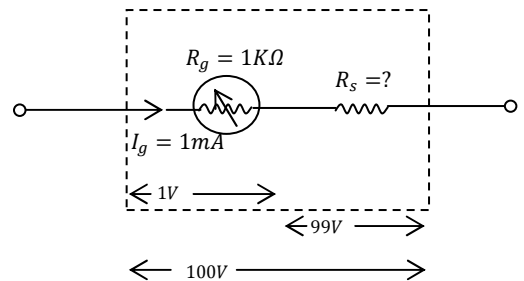
b) In series current is same

$$99V = R_s \times 1mA$$

$$R_s = \frac{99V}{1mA}$$

$R_s = 99K\Omega$

Which can bear 100V



New device can measure 100 volt.